Rate of Change will Is there a time t, $3 \le t \le 6$, at which C'(t) = 1. Justify your answer. equal the Instantaneous Rate of Change

2013 BC3

Hot water is dripping through a coffeemaker, filling a large cup with coffee. The amount of coffee in the cup at time t, $0 \le t \le 6$, is given by a differentiable function C, where t is measured in minutes. Selected values of C(t), measured in ounces, are given in the table.

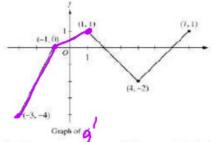
t(minute s)	0	1	2	/3	4	5	6
C(t) ounces	0	5.3	8.8	11.2	12.8	13.8	14.2

Aug Rule of Change

Instantaneous rated change is 1 Slope of tungent line is 1

Let g be a continuous function with g(2) = 5. The graph of the piecewise-linear

g', the derivative of g, is shown for $-3 \le x \le 7$.



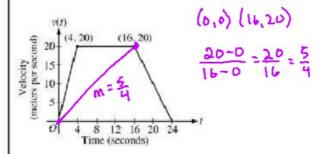
Find the average rate of change of g'(x), on the interval $-3 \le x \le 1$. Does the Mean Value Theorem applied on the interval $-3 \le x \le 1$ guarantee a value of c, for $-3 \le c \le 1$ 1, such that g'(c) is equal to this average rate of change? Why or why not?

A.R.O.C. of g/(x) =
$$\frac{-4-1}{-3-1} = \frac{5}{-4} = \frac{5}{4}$$

A.R.o.c. of $g'(x) = \frac{-4-1}{-3-1} \cdot \frac{-5}{4} = \frac{5}{4}$ No, because g'(x) is not differentiable from [-3,1] -34

2005 AB5

A car is traveling on a straight road. For $8 \le t \le 24$ seconds, the car's velocity v(t), in meters per second, is modeled by the piecewise-linear function defined by the graph



Find the average rate of change of v over the interval $0 \le t \le 16$ Does the Mean Value guarantee a value of c, for 0 < c < 16, such that v(t) is equal to this average rate of change? Why of why not?

No. B/C v(t) is not differential from OLCLIL

2004 BCB3

A test plane flies in a straight line with positive velocity v(t), in miles per minute at time t minutes, where v is a differentiable function of t. Selected values of v(t) are shown.

		\sim		~	(-				
t(min)	0	(5)	10	15	20	25	30	35	40
v(t) (mpm)	7	9.2	9.5	9.2	4.5	2.4	4.5	4.9	7.3

Based on the values in the table, what is the smallest number of instances at which the acceleration of the plane could equal zero on the open interval $0 \le t \le 40$? Justify your answer

Two. Since v(t) is differentiable OL + L4D

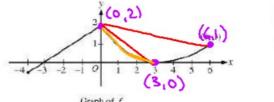
the MuT guarantees the avg. acceleration equals

the instantaneous acceleration

$$\frac{9.2-9.2}{30-20}=0$$

2009 BC3

A continuous function f is defined on the closed interval $-4 \le x \le 6$. The graph of f consists of a line segment and a curve that is tangent to the x-axis at x = 3, as shown in the figure above. On the interval 0 < x < 6, the function f is twice differentiable, with f'(x) > 0.



$$\frac{(0,2)}{a} = \frac{2-1}{0-6} = \frac{1}{-6}$$

Is there a value a, for which the Mean Value Theorem, applied to the interval [a, 6],

guarantees a value c, a < c < 6, at which $f'(c) = \frac{-1}{6}$? Justify your answer. Lycs. a = 0. Since f is differentiable from (0,6) the MuT guarantees that AROC = IROC

2011 BCB5

Ben rides a unicycle back and forth along a straight east-west track. The twicedifferentiable function B models Ben's position of the track, measured in meters from the western end of the track, at time t, measured in seconds from the start of the ride. The table gives values of B(t) and Ben's velocity, v(t), measured in meters per

second, at selected	i times t.			
t(seconds)	0	15	40	60
B(t) (meters)	100	136	9	46
V(t) meters per second	2	2.3	2.5	4.6

Instantaneous v(t)

For $15 \le t \le 60$, must there be a time t when Ben's velocity is -2 meters per second? Justify your answer.

$$\frac{46-136}{60-15} = \frac{-90}{45} = -250$$

yes. since Blt) is differentiable from 02+260 the MVT granates AROLGBLE) = IROLGBLE)

Page 36

Rage CALCULUS: Graphical, Numerical, Algebraic by Finney, Demana, Watts and Kennedy

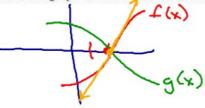
8 2: 1 'Hapitals Rule pg. 444-452 Chapter 8: Applications of Derivatives 8.2: L'Hopitals Rule pg. 444-452

What you'll Learn About:

How to use derivatives to find limits in an indeterminate form

Why L'Hopitals Works

Sketch the graph of two curves with the following characteristic f(2) = g(2) = 0.



a) Write the tangent line for f(x)

a) Write the tangent line for
$$f(x)$$

(2,0) $f'(2)$

(2,0) $g'(2)$

(2,0) $g'(2)$

(2,0) $g'(2)$

(2,0) $g'(2)$

(3,0) $g'(2)$

(4,0) $g'(2)$

c)
$$\lim_{x \to 2} \frac{f(x)}{g(x)} = \frac{f(2)}{g(2)} = \frac{O}{O}$$

= $\frac{O + f'(2)(x-2)}{O + g'(2)(x-2)}$

$$= \frac{0 + f'(2)(x-2)}{0 + g'(2)(x-2)} = \frac{f'(2)}{g'(2)} - \lim_{x \to 2} \frac{f(x)}{g(x)}$$

$$\left| \lim_{x \to 0} \frac{2x^2}{x^2} \right| = 2$$

$$2) \lim_{x\to 0} \frac{\sin(5x)}{x} = \frac{O}{O}$$

$$\lim_{x\to 0} \frac{2x^2}{x^2} = \frac{0}{0}$$

36 | Page

2 Indeterminate Form

V	1	,	3
v			

4)
$$\lim_{x \to 1} \frac{\sqrt[3]{x-1}}{x-1} = \frac{0}{0}$$

A)
$$\lim_{x \to \infty} \frac{x^3 - 1}{4x^3 - x - 3}$$

$$27) \quad \lim_{x \to \infty} \frac{\ln(x^5)}{x}$$

 $\lim_{x \to 1} \frac{3x^2}{12x^2 - 1} = \frac{3}{11}$

49) $\lim_{x\to 1} \frac{x^3-1}{4x^3-x-3} = \frac{0}{0}$

35)
$$\lim_{x \to \infty} \frac{\log_2(x)}{\log_3(x+3)}$$

33)
$$\lim_{x \to 0} \frac{\sin(x^2)}{x} = \frac{O}{O}$$

$$\lim_{x\to 0} \frac{\cos(x^2) \cdot 2x}{1} = 0$$

$$\lim_{X\to 0} \frac{\cos(x^2) \cdot 2x}{1} = 0$$

$$\lim_{X\to 0} \frac{\sin(x^2)}{x} = 0$$

